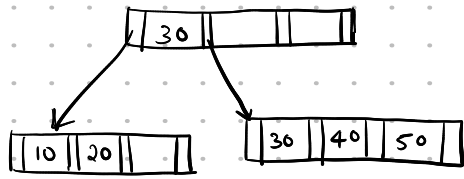
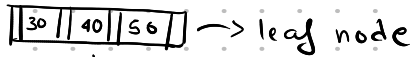


INSERTION

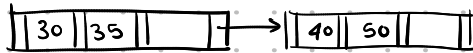


find the leaf node,
leaf node is full so
split the leaf node

insert 35

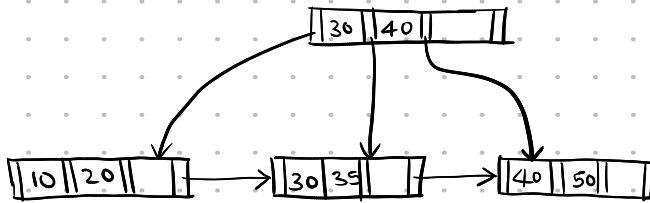


split

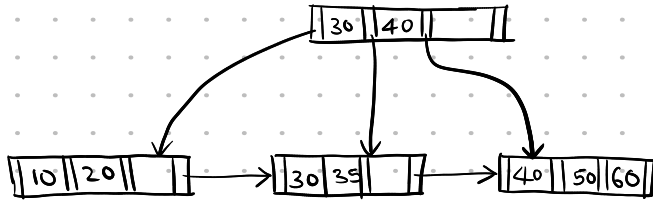


first $\lceil n/2 \rceil$ (ceil) elements
will go to left node and rest go to
new right node

update
parent node

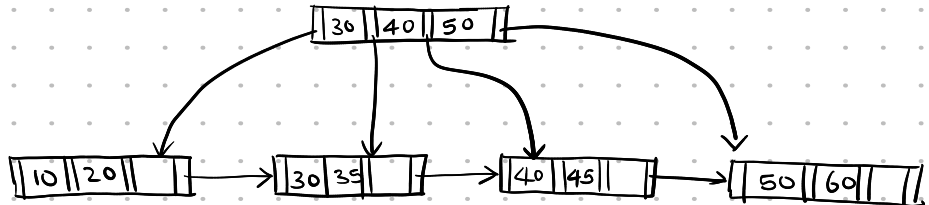


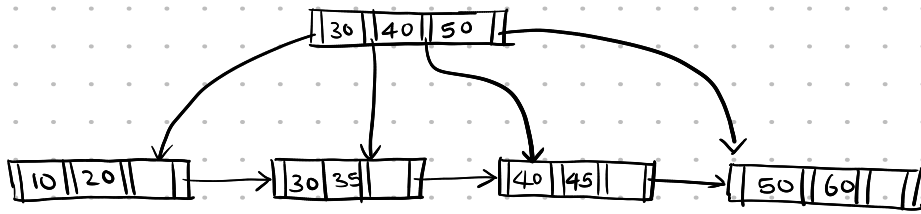
insert 60



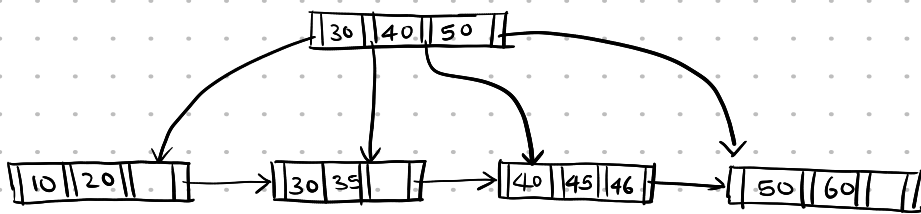
insert 45

leaf nodes are
split just like
before





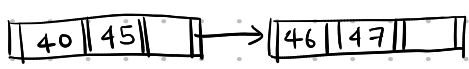
insert 46



insert 47

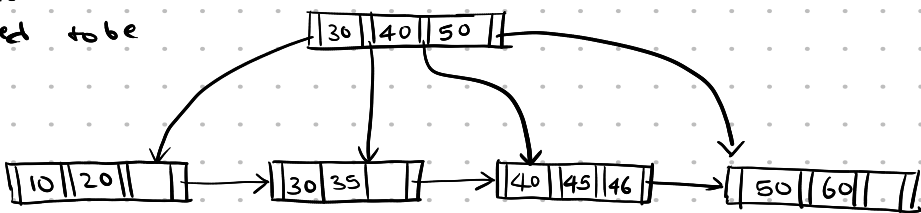
find the node "[40 | 45 | 46]"

split



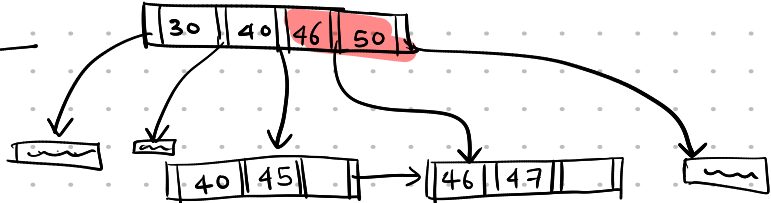
update the parent Node

here the parent node is full and its need to be split it,



extend (Only Conceptual)

assume the parent node is extended and is then split :-



split

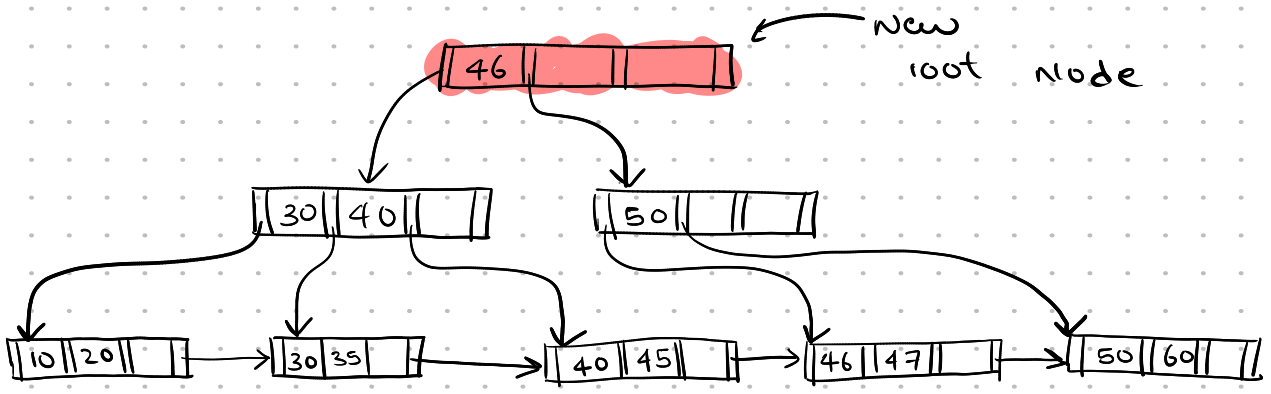


left

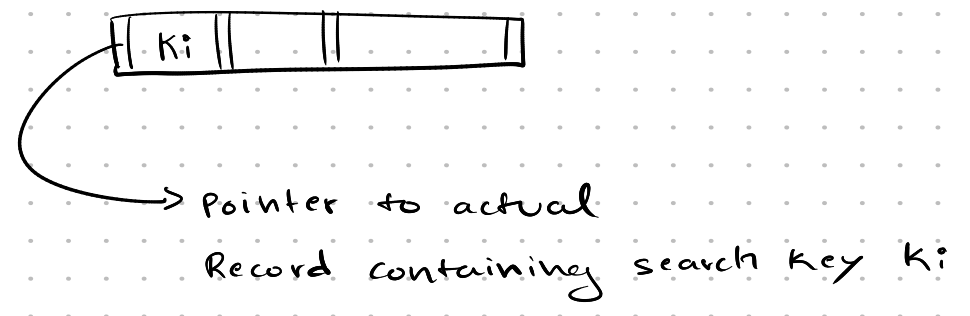
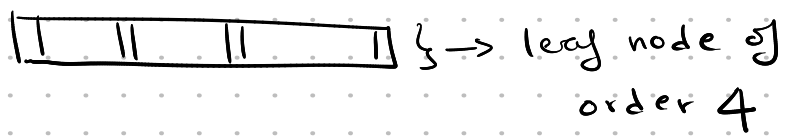
right

move 46 to parent node

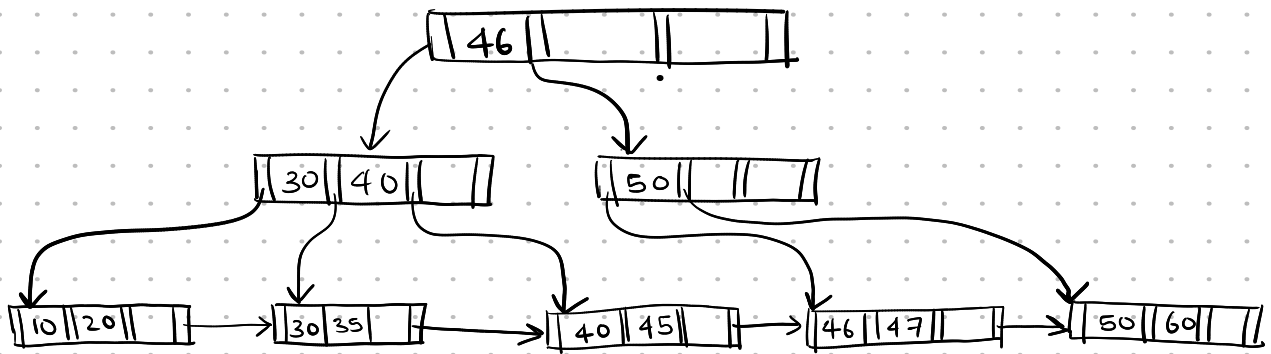
here search key value present b/w pointers which are in kept in the left non leaf-node & the pointers that were moved to right in this case "46", is moved to its parent node but there is no parent node so we create a new node which increases the depth of the B-tree



Structure of leaf node



DELETION



↓ Delete 45

find leaf Node 40 | 45 | |

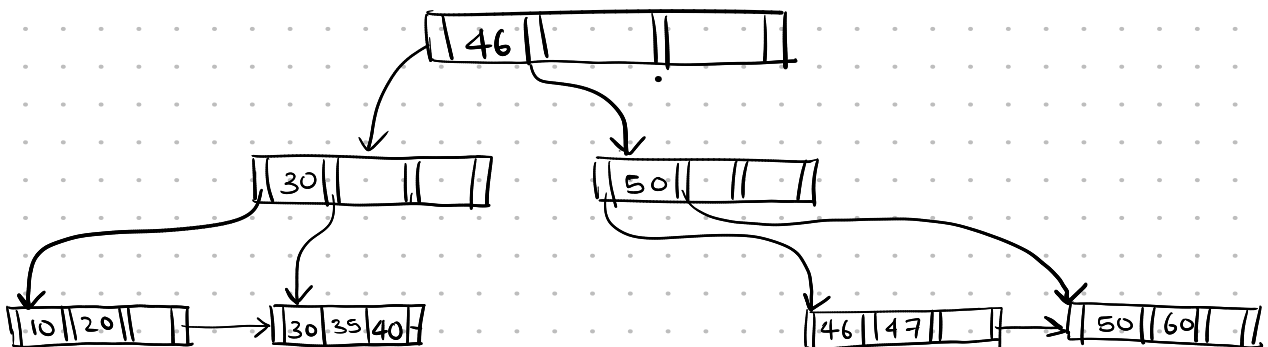
Delete record entry 40 | | |

Now leaf now has

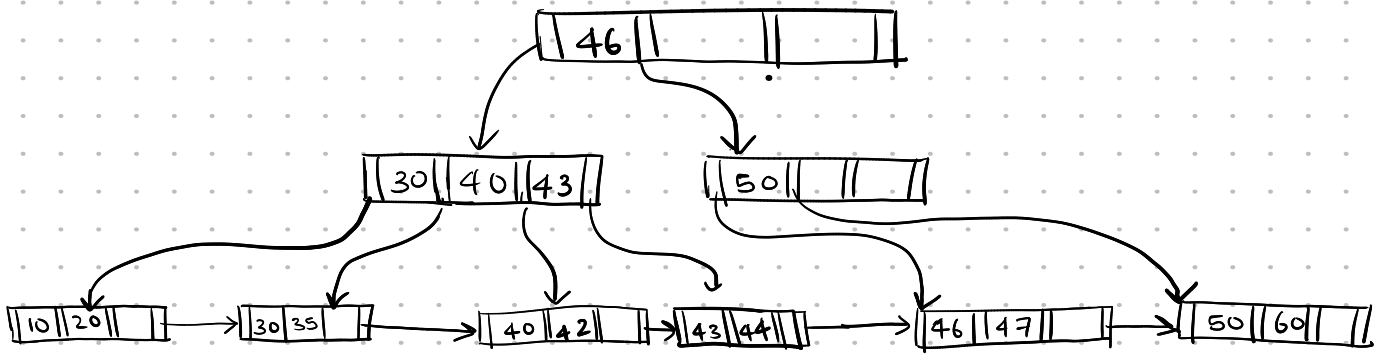
$$n=1, \quad n-1 < \lceil (n-1)/2 \rceil \\ < \lceil 3/2 \rceil \\ 1 < 2$$

so the leaf node must be merged or Redistributed

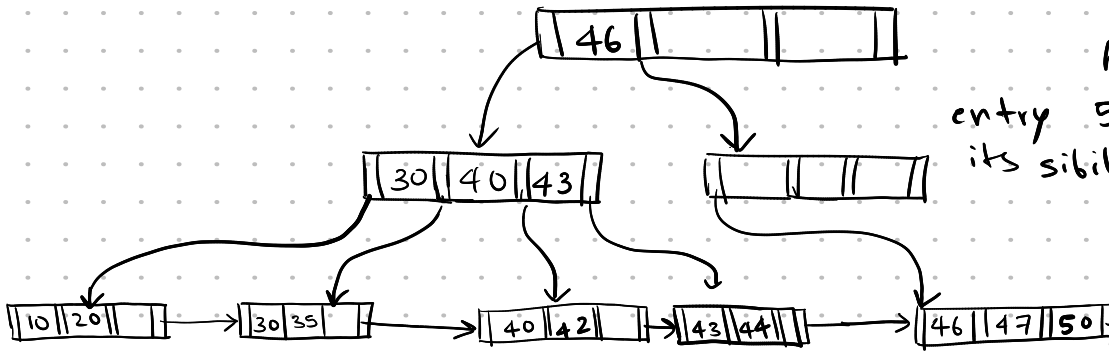
here there is enough space, so the search key "40" is merged with its sibling, and empty node is deleted and the search key in parent node is also deleted



assume the below b-tree



↓ Delete index entry "60"

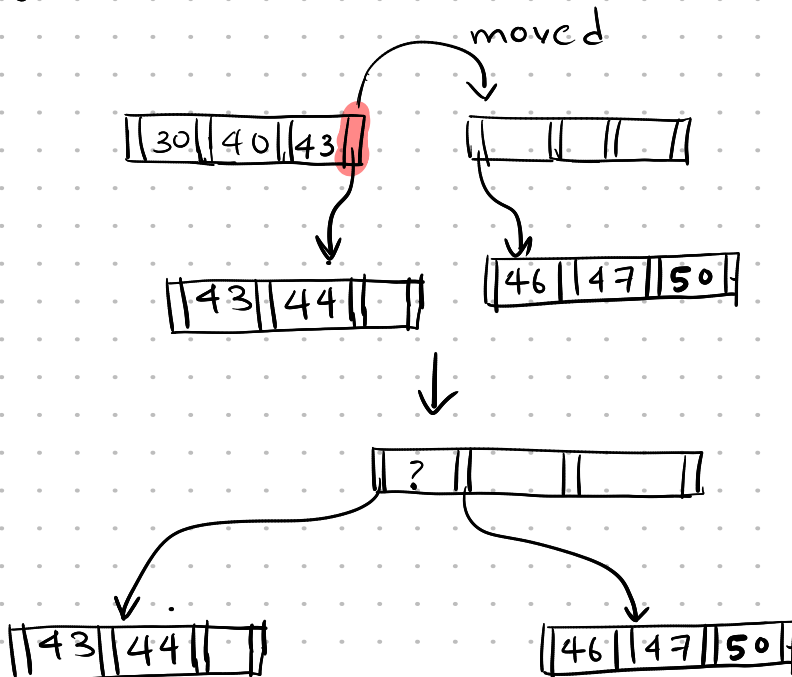


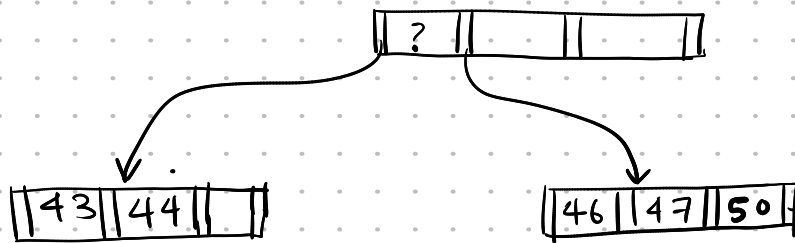
here the index entry 50 is merged with its sibling node,

search key in the Parent is also deleted, which leaves the parent with only one pointer, $n=1$
 ∴ It must be merged or redistributed

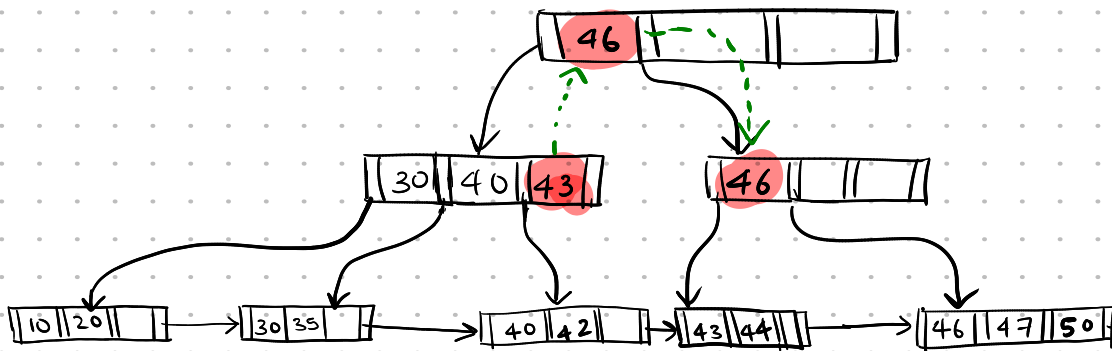
here merging is not possible with the sibling node as it is already full we go with the Redistribution of pointers

right most pointer is moved to the right node

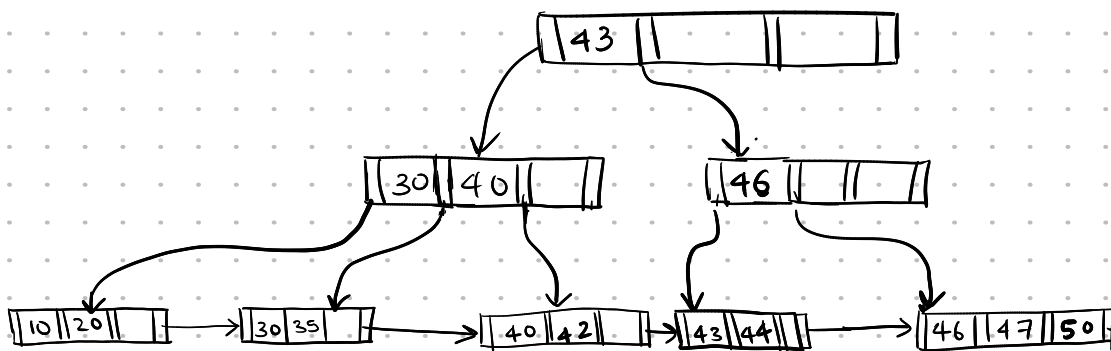




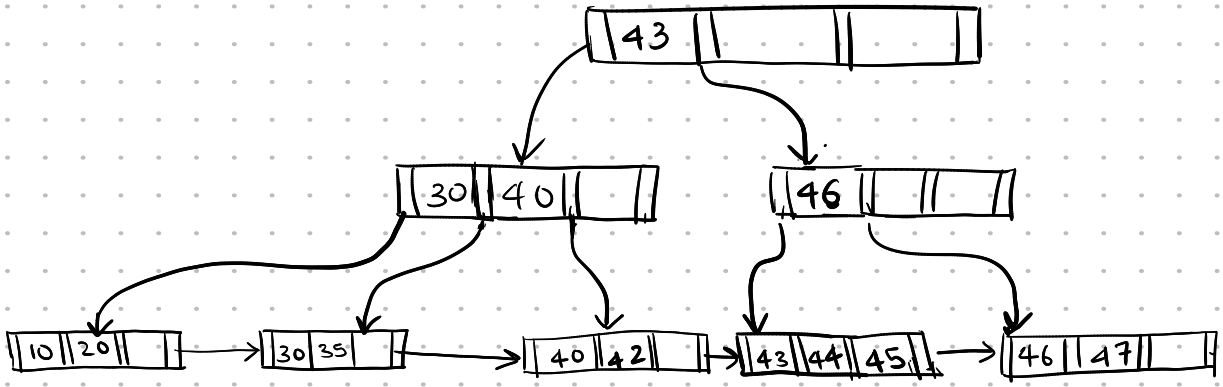
here the value separating these two pointers is not present in both the nodes, but the search key value present in the "parent node" correctly separates them



As the pointers are now redistributed, the parent key no-longer correctly separates the sibling nodes, so the correctly separating key "43" is moved up

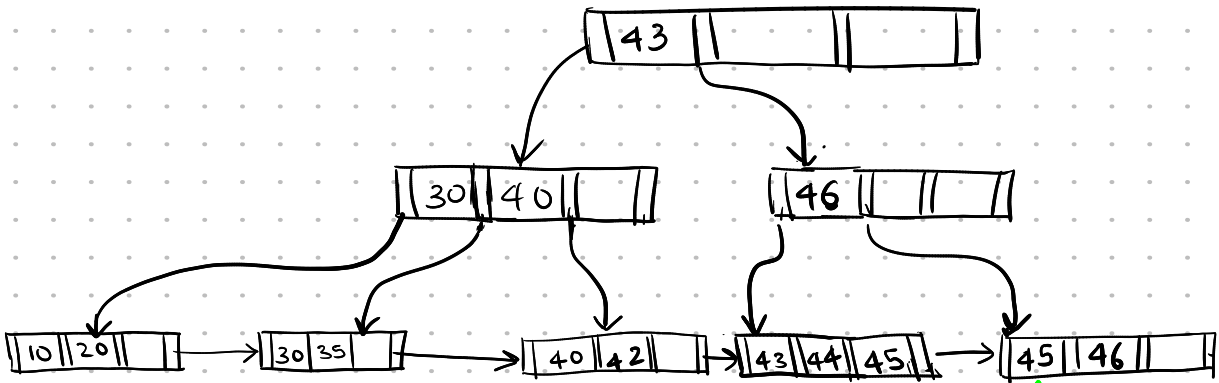


now, assume the below b-tree

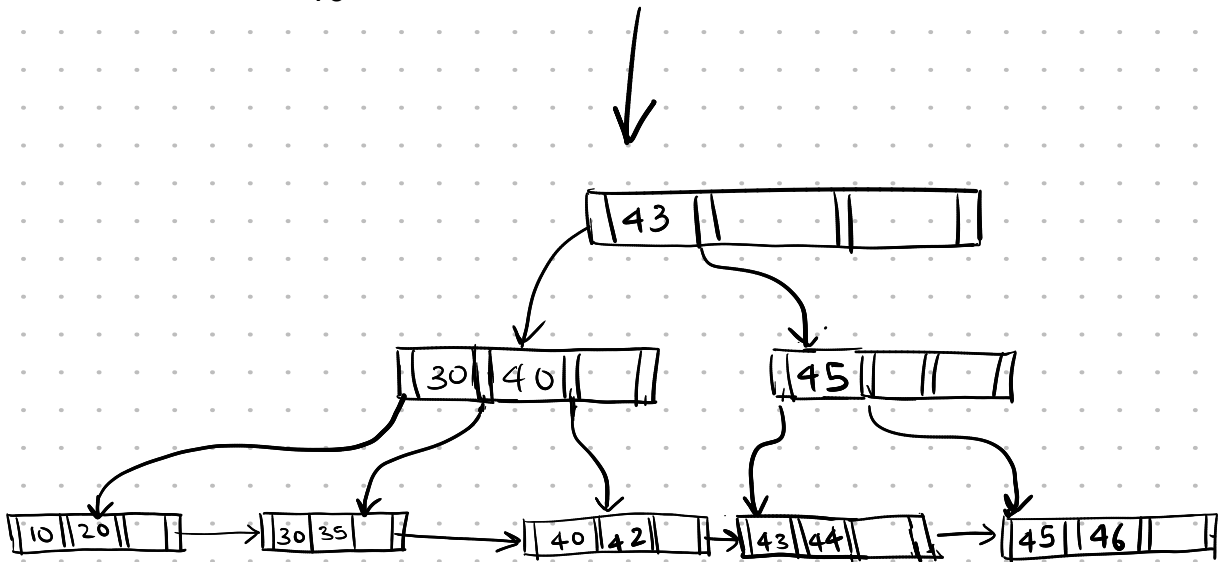


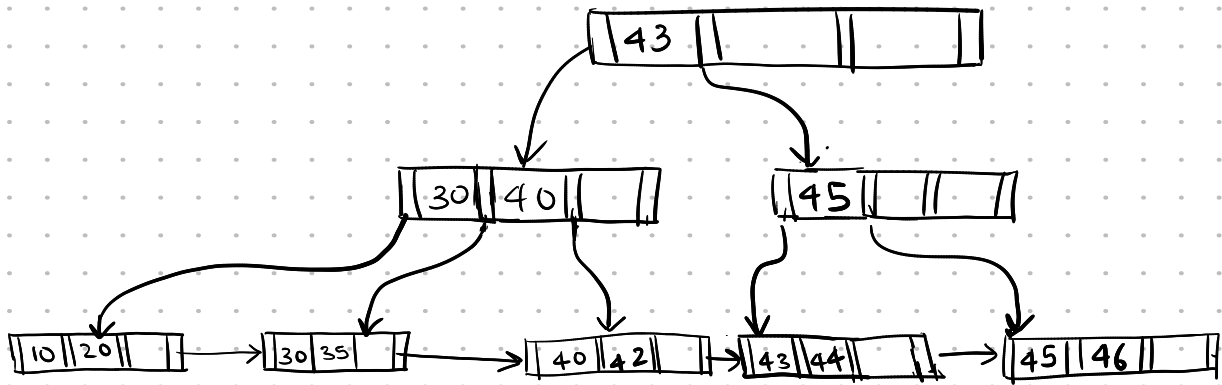
↓ Delete 47

deletion of 47 from the leaf node makes it underfull, now the leaf node cannot be merged with the sibling node as, it is full so we redistribute the nodes, the left most node that is 45 is brought to the right node



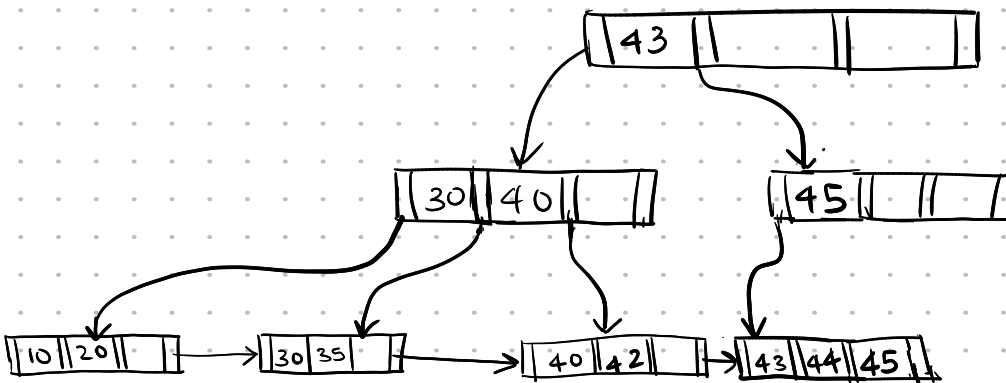
now 46, present in the parent node no longer separates, the two child nodes, so we correct it by changing it to 45





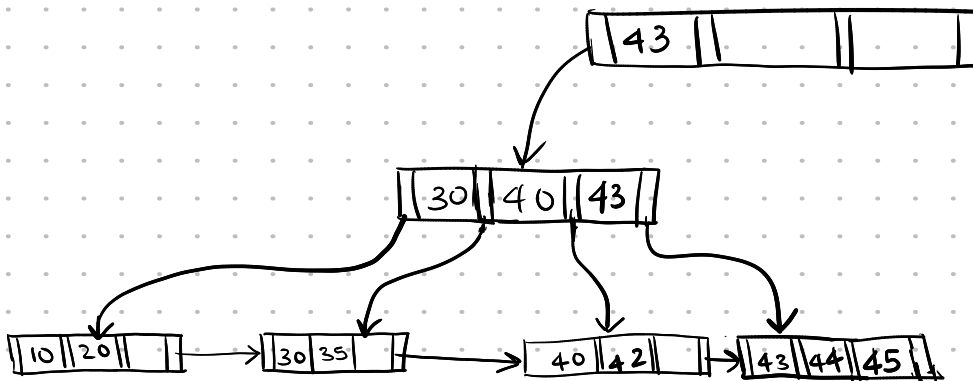
↓ Delete 46

if we delete 46, the index entry 45 can be merged with its' sibling node



now the parent node is underflowing, it can now also be merged with it's sibling, the search key value seperating them is the value present in their parent's node 43

↓



↓ now, the root node contains only one pointer it can have atleast two pointers, so the root node is also remove

